Introduction

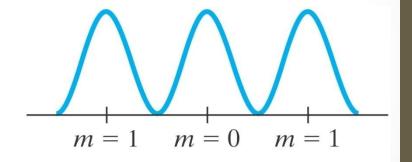
- Diffraction grating can be understood as an optical unit that separates polychromatic light into constant monochromatic composition.
- Uses are tabulated below

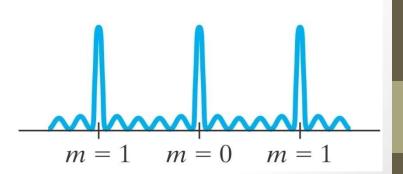
FIELD	USE	
Quantum Mechanics	Verification of Hydrogen spectrum	
Astrophysics	Composition and processes in stars and planetary atmospheres	/
chemistry	Concentration of chemical species in samples	
Telecommunications	Increase the capacity of fiber optic networks using WDM	3

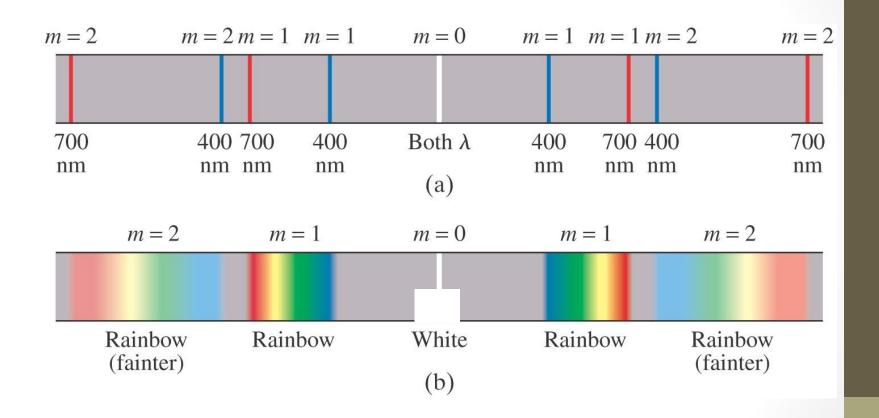
When an Electromagnetic radiation falls on a Diffraction Grating, the electric field and Phase are modified in a predictable manner.

Diffraction Grating A diffraction grating consists of a large number of equally spaced narrow slits or lines. A transmission grating has slits, while a reflection grating has lines that reflect light.

The more lines or slits there are, the narrower the peaks.







Diffraction Grating The maxima of the diffraction pattern are defined by

$$d \sin \theta = m\lambda$$
, $m = 0, 1, 2, ...$

d is the grating width between slits. m denotes the principal maxima.

Diffraction grating: lines.

Determine the angular positions of the first- and second-order maxima for light of wavelength 400 nm and 700 nm incident on a grating containing 10,000 lines/cm.

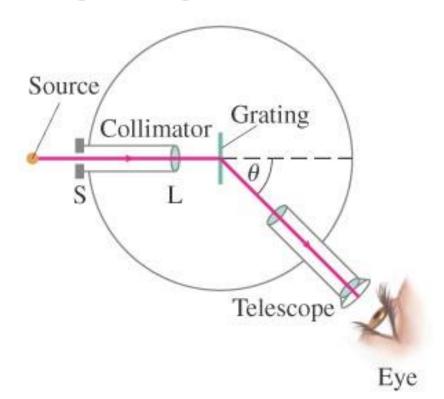
Spectra overlap.

White light containing wavelengths from 400 nm to 750 nm strikes a grating containing 4000 lines/cm. Show that the blue at $\lambda = 450$ nm of the third-order spectrum overlaps the red at 700 nm of the second order.

Compact disk.

When you look at the surface of a music CD, you see the colors of a rainbow. (a) Estimate the distance between the curved lines (to be read by the laser). (b) Estimate the distance between lines, noting that a CD contains at most 80 min of music, that it rotates at speeds from 200 to 500 rev/min, and that 2/3 of its 6-cm radius contains the lines.

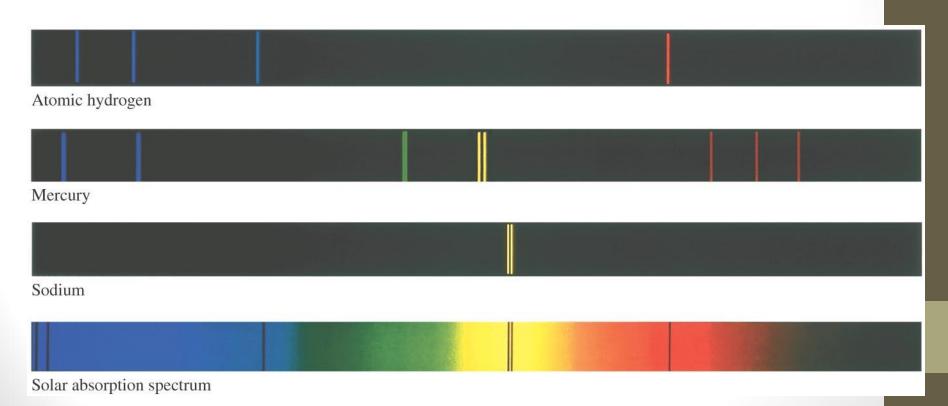
A spectrometer makes accurate measurements of wavelengths using a diffraction grating or prism.



The wavelength can be determined to high accuracy by measuring the angle at which the light is diffracted:

$$\sin \theta = \frac{m\lambda}{d}, \qquad m = 0, 1, 2, \dots$$

Atoms and molecules can be identified when they are in a thin gas through their characteristic emission lines.

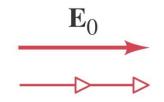


Hydrogen spectrum.

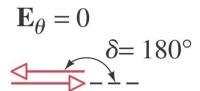
Light emitted by hot hydrogen gas is observed with a spectroscope using a diffraction grating having 1.00 x 10⁴ lines/cm. The spectral lines nearest to the center (0°) are a violet line at 24.2°, a blue line at 25.7°, a blue-green line at 29.1°, and a red line at 41.0° from the center. What are the wavelengths of these spectral lines of hydrogen?

Peak Widths and Resolving Power

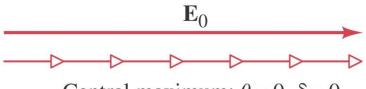
These two sets of diagrams show the phasor relationships at the central maximum and at the first minimum for gratings of two and six slits.



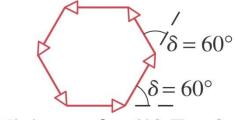
Central maximum: $\theta = 0$, $\delta = 0$



Minimum: δ = 180°



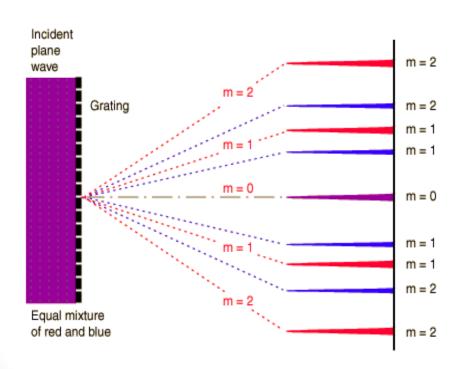
Central maximum: $\theta = 0$, $\delta = 0$

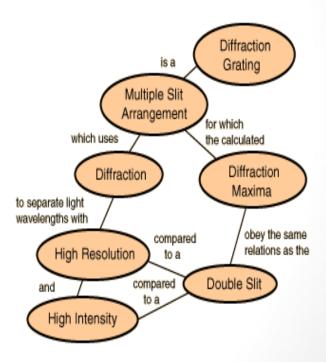


Minimum: $\delta = 60^{\circ}, E_{\theta} = 0$

Physicist view of Diffraction grating

A Multi-slit arrangement which uses diffraction to separate light wavelengths with high resolution and high intensity. The resolving power is achieved by interference of light.





Basics of diffraction

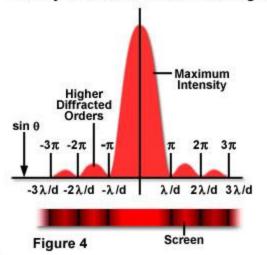
Single slit interference

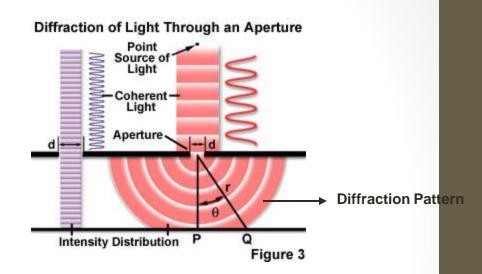
P- 1st maximum

Q- 1st secondary maximum

 $\theta = n\lambda/d$

Intensity Distribution of Diffracted Light





Intensity of the beam is governed by

$$I = I_0 \{ \sin \beta / \beta \}^2$$

Where $\beta = (\pi / \lambda) d \sin \theta$

Two Slit Interference:

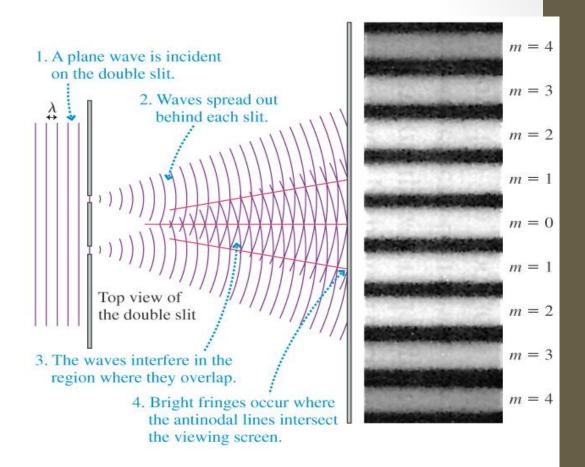
Slit width b

Distance between the slits d

$$I = I_0 \{ \sin \beta / \beta \}^2 \cos^2 \mu$$

Where
$$\beta = (\pi/\lambda)$$
.b sin θ

$$\mu = (\pi/\lambda).d \sin \theta$$



Intensity distribution is similar to single slit and the spacing between the fringes is determined by (λ/d) and width of the envelop by λ/b .

Multiple slit interference

- A N-slits interference pattern is the diffraction pattern and we develop diffraction gratings based on N-slit interference pattern.
- Intensity transmission function is

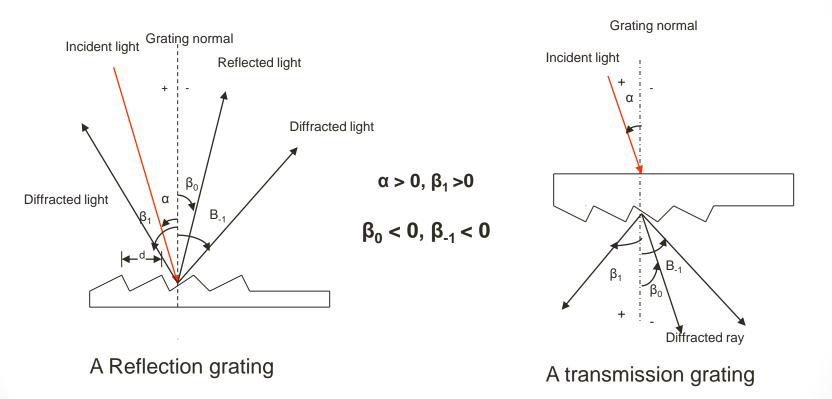
$$I = I_0 \{ \sin \beta / \beta \}^2 \{ (\sin N\mu) / (N \sin \mu) \}^2$$

Where
$$\beta = (\pi/\lambda)$$
.b sin θ
 $\mu = (\pi/\lambda)$.d sin θ

- Principle fringes occur at $\mu = n \pi \rightarrow n \lambda = d \sin \theta$
- Secondary fringes occur at $\mu = 3\pi/2N$, $5\pi/2N$,

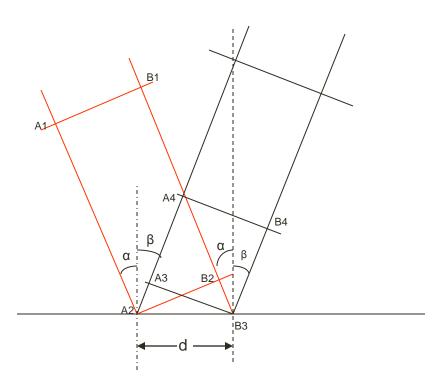
Physics of diffraction

Ray Propagation through the grating



Light diffracted in the same direction of the incident ray → +ve angle

Wave front propagation through the grating



Path difference = A2A3 \sim B2B3 = d sin α + d sin β

Classical diffraction:

Grating equation: $m\lambda = d(\sin\alpha + \sin\beta)$

→ Gm λ = sin α + sin β

→ Gmλ= 2cosK sinØ

G - groove frequency = 1/d

λ – wavelength of the diffracted light

K – deviation angle = $\frac{1}{2}(\alpha-\beta)$

 \emptyset – scan angle = $\frac{1}{2}(\alpha + \beta)$

Littrow configuration : $\alpha = \beta$

→ mλ= 2dsinα

Conical diffraction:

 $Gm\lambda = cos\epsilon (sin\alpha + sin\beta)$

 ε – angle between the incident light path and the plane perpendicular to the grooves.

Characteristics of Diffraction Grating

- Dispersion:

 angular dispersion

 linear dispersion
- Resolving power
- Spectral resolution
- Band pass
- Focal length and f-number
- Anamorphic magnification
- Free spectral range
- Energy distribution

- Scattered and stray light scattered light instrumental stray light
- Signal to noise ratio.

DISPERSION

 Angular Dispersion is the measure of the separation between diffracted light of different wavelengths. It gives the spectral range per unit angle.

Mathematically,

D=
$$\partial \beta/\partial \lambda$$
 = G.m.secβ
= $(2/\lambda)\tan \beta$ --- Littrow condition

Linear dispersion is the product of angular dispersion D and effective focal length
 r'(β)

linear dispersion (I) = $r'D = r'.G.m.sec\beta$

Platefactor is change in wavelength when we move along the spectrum and is given by $P = 1/I = d\cos\beta / r'm$

Obliquity factor is the factor that governs the platefactor when the incident ray is not perpendicular to the grooves and is = $1/\sin\emptyset$

RESOLVING POWER

• This is the ability to separate adjacent spectral lines of average wavelength λ . Mathematically,

$$R = \lambda/\Delta\lambda$$
 $\Delta\lambda$ -- limit of resolution, difference in wavelength of equal intensity

Theoretically, it is the product of diffraction order and the total number of grooves illuminated.

R = N.d.(sinα + sinβ)/
$$\lambda$$
 \rightarrow R_{max} = 2n.d/ λ

SPECTRAL RESOLUTION:

• $\Delta\lambda$ is the spectral resolution and is measured by convoluting the image of the entrance aperture with the exit aperture.